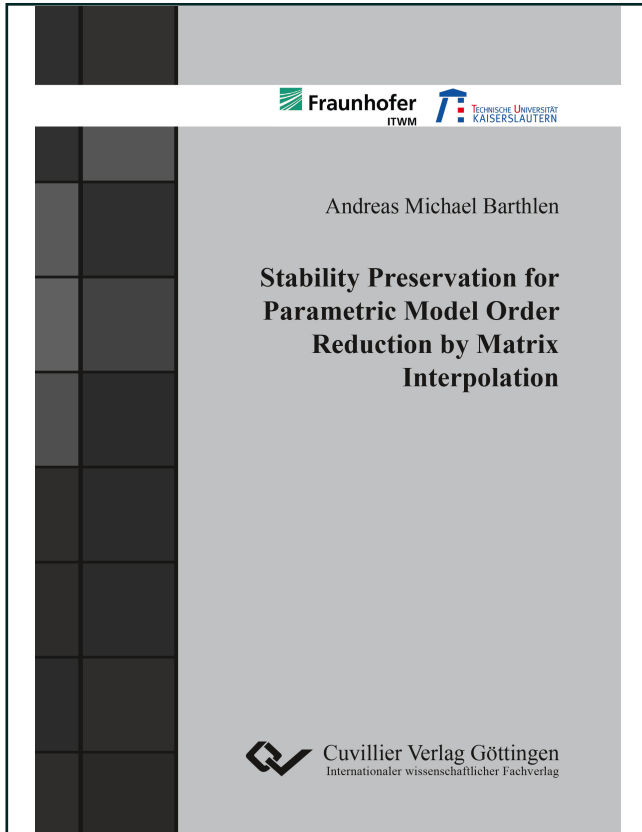




Andreas Michael Barthlen (Autor)

# **Stability Preservation for Parametric Model Order Reduction by Matrix Interpolation**



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