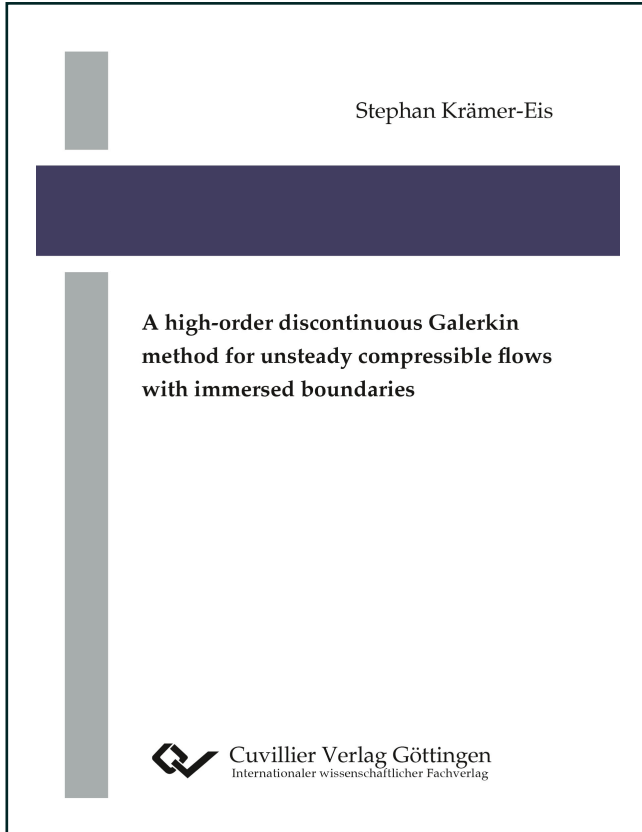




Stephan Krämer-Eis (Autor)

**A high-order discontinuous Galerkin method for unsteady compressible flows with immersed boundaries**



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