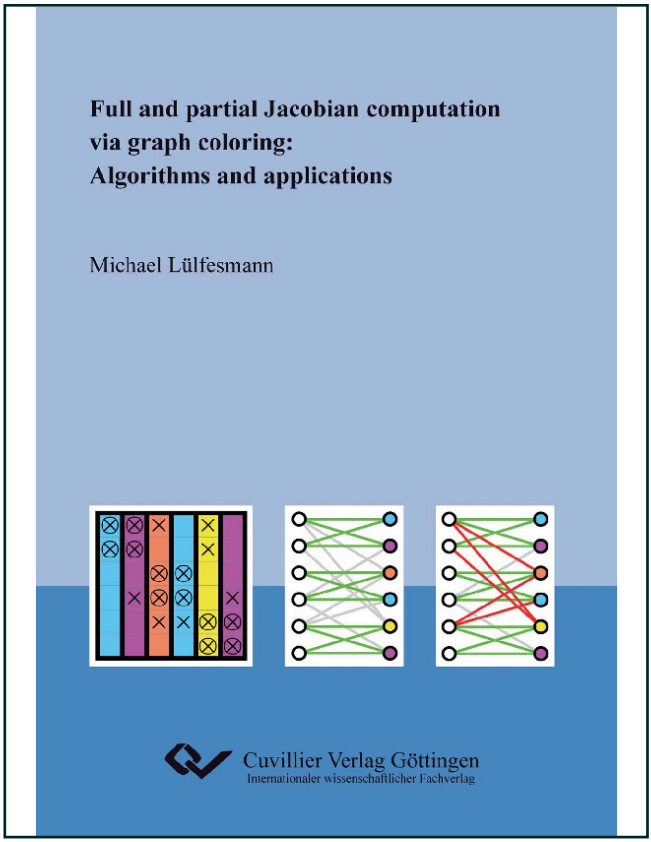
Michael Lülfesmann (Autor)

Full and partial Jacobian computation via graph coloring: Algorithms and applications



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