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## **Band limited Motion Control of CNC Machine Tools**



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Hrsg. Prof. Dr. -Ing. K.Rall

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### **Band Limited Motion Control of CNC Machine Tools**

Von  
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**Band 20**

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# Table of Contents

<b>Abstract</b>	<b>i</b>
<b>Nomenclature</b>	<b>xi</b>
<b>Acronyms</b>	<b>xvii</b>
<b>Glossary of some frequently related technical terms</b>	<b>xix</b>
<b>1 Introduction</b>	<b>1</b>
1.1 Motivation . . . . .	1
1.2 Problem Description and Aims . . . . .	3
1.3 Overview of the Thesis . . . . .	7
<b>2 CNC controlled Machine Tools</b>	<b>9</b>
2.1 Motion Planning and Control . . . . .	10
2.1.1 Basic functions of the NC kernel . . . . .	10
2.1.2 Trajectory planning . . . . .	11
2.2 Servo Control . . . . .	17
2.2.1 Cascade control . . . . .	18
2.2.2 Feedforward control . . . . .	20
2.2.3 State space control . . . . .	22
2.3 Mechanical Systems . . . . .	22
2.3.1 Mechanical System Modeling . . . . .	23
2.3.2 Test Rig setup . . . . .	25
2.3.3 Motion control architecture of the test rig . . . . .	25

## TABLE OF CONTENTS

---

<b>3</b>	<b>Cascade Control with Input Shaper</b>	<b>29</b>
3.1	Designing Parameters of Controllers for Elastic System . . . . .	30
3.1.1	Designing parameters of controllers in the velocity loop . . . . .	30
3.1.2	Designing the parameter of the controller in position loop . . . . .	39
3.2	Input Shaper . . . . .	41
3.2.1	Input shaper in time domain . . . . .	42
3.2.2	Input shaper in the frequency domain . . . . .	44
3.2.3	Sensitivity of input shaper . . . . .	47
3.3	Designing Cascade Control Loop with Input Shaper . . . . .	49
3.3.1	Designing Input Shaper for closed velocity loop . . . . .	50
3.4	Brief Summary of Chapter 3 . . . . .	56
<b>4</b>	<b>System Parameters Identification</b>	<b>59</b>
4.1	Transfer Function . . . . .	61
4.1.1	For second order system ( $n=1$ ) . . . . .	63
4.1.2	For third order system ( $n=2$ ) . . . . .	64
4.1.3	For fourth order system ( $n=3$ ) . . . . .	66
4.1.4	For $n^{th}$ order system . . . . .	67
4.2	Parameter Identification in Frequency Domain . . . . .	68
4.2.1	For second order system ( $n=1$ ) . . . . .	70
4.2.2	For third order system ( $n=2$ ) . . . . .	71
4.2.3	For fourth order system ( $n=3$ ) . . . . .	72
4.2.4	For $(n + 1)^{th}$ order system . . . . .	76
4.2.5	Results and simulations . . . . .	80
<b>5</b>	<b>Trajectory Analysis and Trajectory Redesign through Wavelet Synthesis</b>	<b>83</b>
5.1	Time Frequency Analysis . . . . .	84
5.1.1	Short Time Fourier Transform . . . . .	85
5.1.2	Multi-resolution Short Time Fourier Transform . . . . .	87
5.1.3	Wavelet Transform . . . . .	88
5.1.4	Comparison . . . . .	95
5.2	Predicting Vibraton Level Along Time . . . . .	96

## TABLE OF CONTENTS

---

5.2.1	Second order system response . . . . .	97
5.2.2	Amplitude error calculation of the response of a second-order system by Wavelet Synthesis . . . . .	99
5.2.3	Summary of amplitude error calculation by Wavelet Synthesis . . . . .	109
5.3	Resonance Frequency Reduced Trajectory . . . . .	110
5.3.1	Reduction of vibration in axis motion . . . . .	110
5.3.2	Process of Redesign . . . . .	112
5.4	Simulation Results . . . . .	115
<b>6</b>	<b>Examples and Experiments</b>	<b>119</b>
<b>7</b>	<b>Conclusions</b>	<b>125</b>
<b>A</b>	<b>Appendix</b>	<b>129</b>
A.1	Calculation of the Test Rig's Parameters . . . . .	129
A.2	For fifth order system (n=4) . . . . .	132
A.3	Following Errors in the Experiments . . . . .	137
	<b>References</b>	<b>140</b>