

# Contents

<b>1</b>	<b>Introduction</b>	<b>5</b>
1.1	Organization of this Thesis . . . . .	7
<b>2</b>	<b>Exploratory Data Analysis</b>	<b>9</b>
2.1	Knowledge Discovery . . . . .	10
2.2	Visual Data Mining . . . . .	11
2.2.1	Scientific Visualization . . . . .	13
2.2.2	The Process of Scientific Visualization . . . . .	14
2.2.3	Classification Schemes for Scientific Data . . . . .	15
2.2.4	Scientific Visualization Techniques . . . . .	17
2.2.4.1	Two-Dimensional Domain . . . . .	18
2.2.4.2	Three-Dimensional Domain . . . . .	21
2.2.5	Color in Visualization . . . . .	24
2.2.5.1	Color Fundamentals . . . . .	25
2.2.5.2	Device Independent Color Spaces . . . . .	26
2.2.5.3	Device Dependent Color Spaces . . . . .	27
2.2.5.4	Color Scale Properties . . . . .	28
2.2.5.5	Univariate Color Scales . . . . .	29
2.2.5.6	Perceptually Optimized Color Mapping Techniques . . . . .	30
2.2.5.7	CIELUV Color Scales Based on sRGB Color Specifications	32
2.2.5.8	Bivariate and Trivariate Color Scales . . . . .	33
2.3	Image Fusion . . . . .	33
2.3.1	Dimensionality Reduction . . . . .	36
2.3.2	Feature Selection . . . . .	38
2.3.3	Feature Extraction . . . . .	38
2.4	Conclusion . . . . .	40
<b>3</b>	<b>Linear Transformations</b>	<b>41</b>
3.1	Principal Component Analysis . . . . .	42
3.1.1	Intrinsic Data Dimensionality . . . . .	45
3.1.2	Eigenvector Computation Using Neural Networks . . . . .	46
3.1.3	Principal Component Analysis and Image Fusion . . . . .	47
3.1.4	Case Study: DCE-MRI of the Breast . . . . .	49
3.1.4.1	Motivation . . . . .	49
3.1.4.2	Detection and Classification of Lesions . . . . .	51
3.1.4.3	Computer Aided Diagnosis . . . . .	53

3.1.4.4	Material and Methods . . . . .	55
3.1.4.5	Preparation of the Data . . . . .	56
3.1.4.6	Experimental Results . . . . .	57
3.2	Procrustes Analysis . . . . .	70
3.2.1	Comparison of Point Configurations . . . . .	70
3.2.2	Comparison of Subspaces . . . . .	71
3.2.3	Case Study Revisited: DCE-MRI of the Breast . . . . .	73
3.2.3.1	Experimental Results . . . . .	73
3.3	Independent Component Analysis . . . . .	77
3.3.1	Statistical Independence . . . . .	78
3.3.2	Non-Gaussianity . . . . .	79
3.3.3	The FastICA Algorithm . . . . .	81
3.3.4	Validation of Independent Components . . . . .	82
3.3.5	ICA and Image Fusion . . . . .	86
3.3.6	Case Study Revisited: DCE-MRI of the Breast . . . . .	88
3.3.6.1	Experimental Results . . . . .	89
3.4	Conclusion . . . . .	97
<b>4</b>	<b>Non-Linear Transformations</b>	<b>99</b>
4.1	Self-Organizing Maps . . . . .	100
4.1.1	The Incremental Algorithm . . . . .	101
4.1.2	Topology Preservation . . . . .	103
4.1.3	Intrinsic Data Dimensionality . . . . .	106
4.1.4	SOM Based Data Visualization . . . . .	108
4.1.4.1	Analysis of the Structure of a Data Distribution . . . . .	108
4.1.4.2	Reference Vector Based Analysis . . . . .	109
4.1.4.3	SOM Calibration . . . . .	109
4.1.5	Image Fusion and Self-Organizing Maps . . . . .	110
4.1.6	Case Study: Screening of Synthetic Stationary-Phase Promoters .	111
4.1.6.1	Motivation . . . . .	111
4.1.6.2	Material and Method . . . . .	112
4.1.6.3	Experimental Results . . . . .	115
4.2	Hyperbolic Self-Organizing Maps . . . . .	118
4.2.1	Characteristics of Hyperbolic Spaces . . . . .	119
4.2.2	The Poincaré Disc Model . . . . .	121
4.2.3	A Hyperbolic Lattice and a Modified Adaptation Method . . . . .	121
4.2.4	Visualizing Hyperbolic Self-Organizing Maps . . . . .	122
4.2.5	The Hyperbolic Self-Organizing Maps in Image Fusion . . . . .	123
4.2.6	Case Study Revisited: DCE-MRI of the Breast . . . . .	124
4.2.6.1	Experimental Results . . . . .	124
4.3	Topographic Mapping for Proximity Data . . . . .	135
4.3.1	Probabilistic Autoencoders . . . . .	136
4.3.2	EM Algorithm and Deterministic Annealing for Optimization . . .	137

4.3.2.1	An Approximation of the Optimization Scheme . . . . .	138
4.3.2.2	A Hyperbolic Topographic Mapping for Proximity Data .	138
4.3.3	Case Study Revisited: DCE-MRI of the Breast . . . . .	140
4.3.3.1	Material and Methods . . . . .	141
4.3.3.2	Experimental Results for the Exploration of Randomly Sampled Image Sections . . . . .	143
4.3.3.3	Experimental Results for Image Fusion based on Proxim- ity Data . . . . .	147
4.4	Conclusion . . . . .	155
<b>5</b>	<b>Summary and Outlook</b>	<b>157</b>
<b>6</b>	<b>Appendix</b>	<b>161</b>
6.1	Performance Metrics . . . . .	161
<b>Bibliography</b>		<b>167</b>