

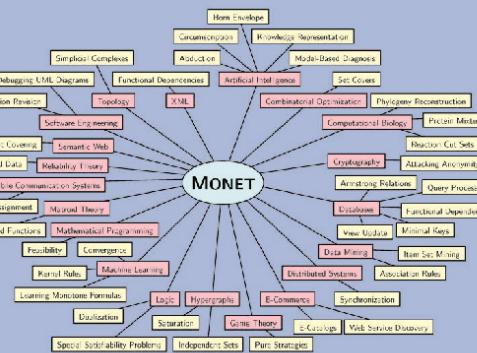


Matthias Hagen (Autor)

"Algorithmic and Computational Complexity Issues of MONET

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