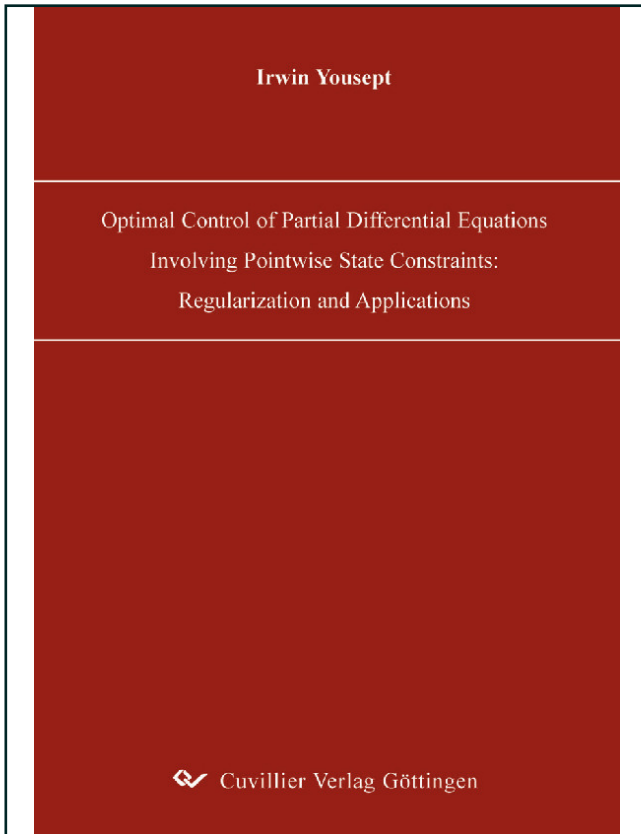




Irwin Yousept (Autor)

**Optimal Control of Partial Differential Equations  
Involving Pointwise State Constraints: Regularization  
and Applications**



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