

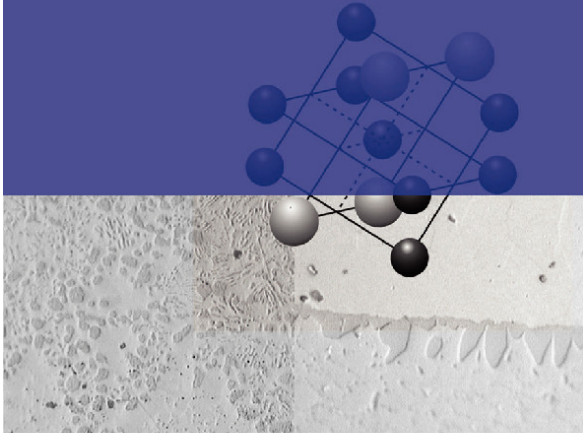


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Investigations of Microstructural Changes in Lead-Free Solder Alloys by Means of Phase Field Theories

Schriftenreihe des Lehrstuhls für Kontinuumsmechanik und Materialtheorie
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