

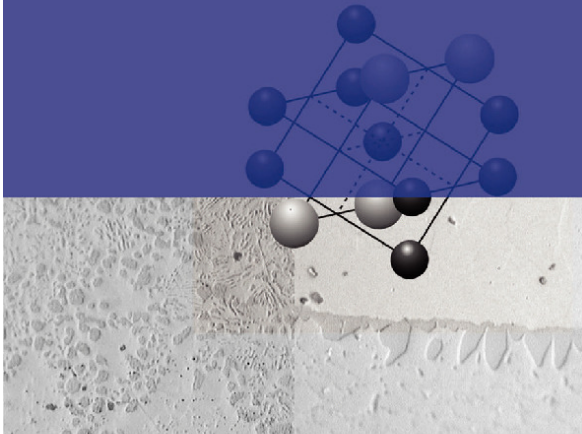


Thomas Böhme (Autor)

Investigations of Microstructural Changes in Lead-Free Solder Alloys by Means of Phase Field Theories

Schriftenreihe des Lehrstuhls für Kontinuumsmechanik und Materialtheorie
der Technischen Universität Berlin

Herausgegeben von Prof. Dr. rer. nat. Wolfgang H. Müller



Thomas Böhme

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