



Tamara Saskia Nunner (Autor)
Spin Excitations in Low-Dimensional Quantum Antiferromagnets

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Quantum Antiferromagnets**



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