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**Frequency Assignment in GSM Networks: Models,
Heuristics and Lower Bounds**

Andreas Eisenblätter

Frequency Assignment
in GSM Networks

Models, Heuristics, and Lower Bounds



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Contents

Preface	v
1 Introduction	1
2 Frequency Planning in GSM	5
2.1 A Brief History of GSM	5
2.2 The General System for Mobile Communications	9
2.2.1 Mobile Stations	9
2.2.2 Subsystems	10
2.2.3 Network Dimensioning	12
2.2.4 Along the Radio Interface	14
2.3 Automatic Frequency Planning	18
2.3.1 Objective and Constraints	20
2.3.2 Precise Data	25
2.3.3 Practical Aspects	30
3 Mathematical Models	33
3.1 The Model FAP	33
3.1.1 Variants	37
3.1.2 Alternative Models	40
3.2 Computational Complexity	42
3.2.1 Preliminaries	42
3.2.2 Classical Problems related to FAP	46
3.2.3 Complexity of FAP	48
3.3 Alternative Formulations	49
3.3.1 Stable Set Model	50
3.3.2 Orientation Model	51
4 Fast Heuristic Methods	55
4.1 Preprocessing	57
4.1.1 Eliminating Channels and Carriers	57
4.1.2 Tightening the separation	59
4.2 Greedy Methods	60
4.2.1 T-Coloring	60

4.2.2	Dsatur With Costs	62
4.2.3	Dual Greedy	64
4.3	Improvement Methods	66
4.3.1	Iterated 1-OPT	67
4.3.2	Variable Depth Search	68
4.3.3	k-Opt	70
4.3.4	Min-Cost Flow	72
5	Computational Studies	77
5.1	Benchmarks	78
5.1.1	Test Instances	79
5.1.2	Threshold Accepting	87
5.2	Analysis of Greedy Heuristics	90
5.2.1	T-Coloring	90
5.2.2	DSATUR with Costs	92
5.3	Analysis of Improvement Heuristics	95
5.3.1	Iterated 1-Opt	96
5.3.2	Variable Depth Search	98
5.3.3	k-Opt	102
5.3.4	Min-Cost Flow	104
5.3.5	Comparisons	104
5.4	Combinations of Heuristics	105
5.5	Selected Results for all Benchmark Scenarios	107
5.6	Conclusions and Challenges	112
6	Quality of Frequency Plans	117
6.1	Relaxed Frequency Planning	118
6.2	Minimum k -Partition	120
6.2.1	Interference is not essentially metric	122
6.2.2	An ILP formulation and a SDP relaxation	124
6.3	Numerical Bounds and Quality Assessments	128
6.4	Relaxed and Ordinary Frequency Planning	131
6.4.1	Feasible Permutations	131
6.4.2	Tours without shortcuts	134
6.4.3	Computational Results	136
6.5	Conclusions	138
7	Partition Polytopes	141
7.1	Binary Linear Programs	142
7.2	The Polytope $\mathcal{P}(K_n)$	145
7.2.1	2-chorded Inequalities	146

7.2.2	Clique-web Inequalities and Special Cases	148
7.2.3	Partition and Claw Inequalities	151
7.3	The Polytope $\mathcal{P}_{\leq k}(K_n)$	152
7.3.1	Inequalities with right-hand side independent of k .	154
7.3.2	Hypermetric Inequalities and Special Cases	155
7.3.3	Cycle Inequalities	161
7.4	Separating Violated Valid Inequalities	163
8	Semidefinite Relaxation of Minimum k-Partition	169
8.1	Preliminaries	169
8.2	Semidefinite Programming	176
8.3	The Minimum k -Partition Relaxation	182
8.4	The semidefinite relaxation $\Theta_{k,n}$ and $\mathcal{P}_{\leq k}(K_n)$	187
8.5	Summary and Outlook	199
A	Notation	201
	Bibliography	207
	Index	219
	Summary in German/Zusammenfassung	225
	Curriculum Vitae/Lebenslauf	227