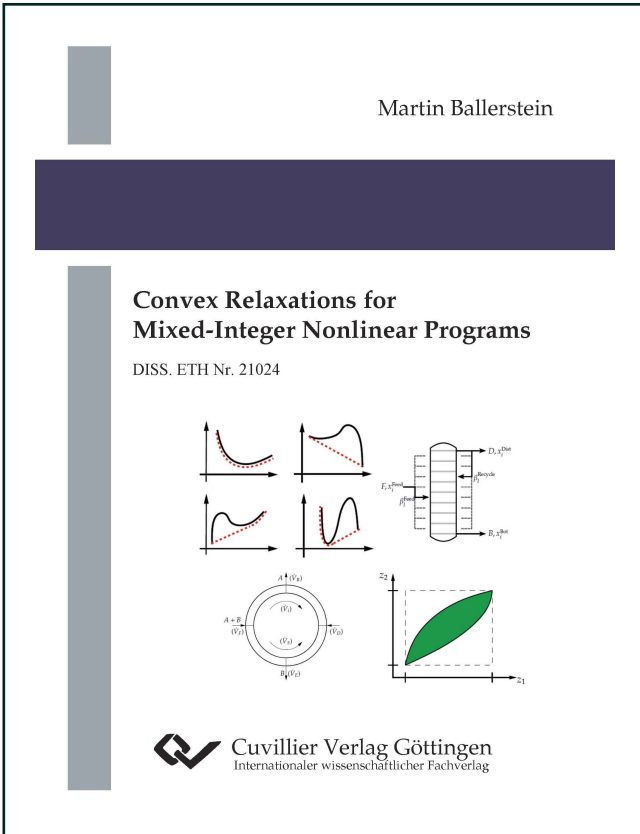




Martin Ballerstein (Autor)
Convex Relaxations for Mixed-Integer Nonlinear Programs



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