



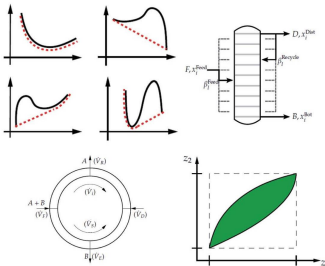
Martin Ballerstein (Autor)

Convex Relaxations for Mixed-Integer Nonlinear Programs

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