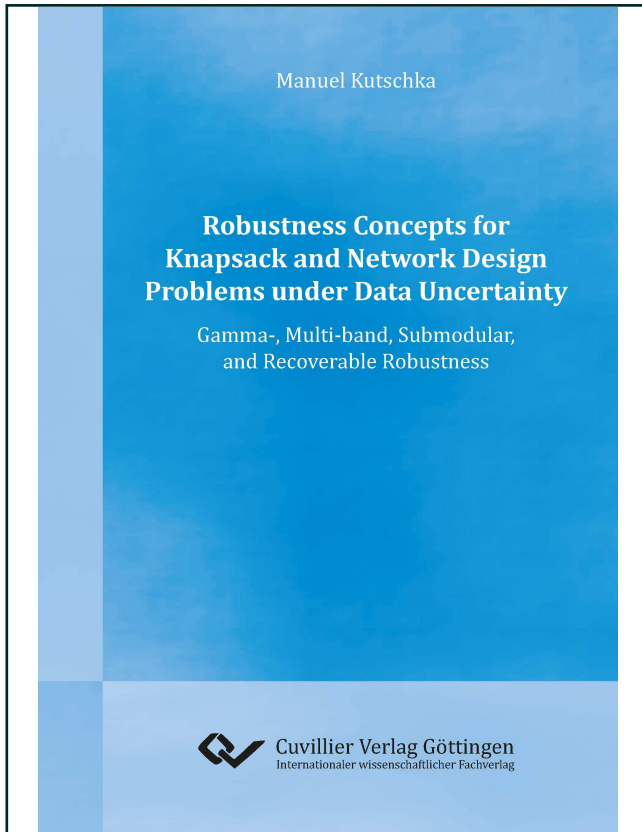




Manuel Kutschka (Autor)

**Robustness Concepts for Knapsack and Network Design
Problems under Data Uncertainty**

Gamma-, Multi-band, Submodular, and Recoverable Robustness



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CONTENTS

Abstract	iii
Zusammenfassung	v
Danksagung	vii
Contents	ix
Introduction	1
I Concepts	5
1 Mathematical preliminaries	7
1.1 Basics	7
1.2 The knapsack problem	14
1.3 The capacitated network design problem	20
1.4 Applications in telecommunication	27
2 Optimization under data uncertainty	35
2.1 Stochastic optimization	36
2.2 Robust optimization	37
2.2.1 Uncertainty sets	38
2.2.2 Tractability of robust optimization problems	41
2.3 Multi-stage optimization under data uncertainty	42
2.3.1 Multi-stage stochastic optimization	43
2.3.2 Multi-stage robust optimization	43
3 Robustness concepts	45
3.1 Γ -robustness	45
3.1.1 The concept of Γ -robustness	46
3.1.2 The Γ -robust counterpart	48
3.1.3 Probabilistic analysis and feasibility guarantees	50



3.2	Multi-band robustness	51
3.2.1	The concept of multi-band robustness	52
3.2.2	The multi-band robust counterpart	55
3.2.3	Probabilistic analysis	57
3.3	Submodular robustness	57
3.3.1	The concept of submodular robustness	58
3.3.2	The submodular robust counterpart	59
3.3.3	Submodular functions: Γ - and multi-band robustness	60
3.4	Recoverable robustness	61
3.4.1	The concept of recoverable robustness	62
3.4.2	The recoverable robust counterpart	63
3.5	Evaluation of robustness	64
II	Robust Knapsack Problems	69
4	The Γ-robust knapsack problem	71
4.1	Formulations	72
4.2	Polyhedral study	73
4.2.1	Basic characteristics	73
4.2.2	Valid inequalities	74
4.3	Algorithms	76
4.3.1	Separation of violated Γ -robust (extended) cover inequalities	76
4.3.2	Solving the Γ -RKP	78
5	The multi-band robust knapsack problem	79
5.1	Formulations	80
5.2	Polyhedral study	81
5.2.1	Basic characteristics	81
5.2.2	Valid inequalities	82
5.3	Algorithms	83
5.3.1	Separation of multi-band robust strengthened extended cover inequalities	84
6	The submodular knapsack problem	85
6.1	Formulations	86
6.2	Polyhedral study	87
6.2.1	Basic characteristics	87
6.2.2	Valid inequalities	87
7	The recoverable robust knapsack problem	95
7.1	Formulations	97
7.2	Polyhedral study	102
7.2.1	Basic characteristics	103



7.2.2	Valid inequalities	105
7.3	Algorithms	111
7.3.1	Solving the Maximum Weight Set Problem	111
7.3.2	Separation of violated recoverable robust extended cover inequalities	112
7.3.3	Solving the RRKP: an approach using robustness cuts	117
8	Computational studies	121
8.1	Instances	122
8.2	Robustness parameters	123
8.3	Results for the $k, \ell/D$ -RRKP	123
8.4	Results for the k/Γ -RRKP	126
III	Robust Network Design Problems	135
9	The Γ-robust network design problem	137
9.1	Formulations	139
9.2	Polyhedral study	143
9.2.1	Basic characteristics	144
9.2.2	Cutset-based inequalities	145
9.2.3	Γ -robust arc residual capacity inequalities	156
9.2.4	Γ -robust metric inequalities	160
9.3	Algorithms	165
9.3.1	Separation of cutset-based inequalities	165
9.3.2	Separation of Γ -robust arc residual capacity inequalities	167
9.3.3	Separation of Γ -robust metric inequalities	170
10	The multi-band robust network design problem	175
10.1	Formulations	176
10.2	Polyhedral study	179
10.2.1	Basic characteristics	180
10.2.2	Cutset-based inequalities	181
10.3	Algorithms	185
10.3.1	Separation of multi-band robust cutset inequalities.	185
10.3.2	Separation of multi-band robust length inequalities	186
11	Computational studies	189
11.1	Instances	189
11.2	Robustness parameters	193
11.3	Comparison of formulations	194
11.4	Strength of valid inequalities	196
11.5	Speed-up of the compact link flow formulation	199
11.6	Speed-up of the capacity formulation	201
11.7	Handling large instances using the capacity formulation	203



11.8 Quality of optimal robust network designs	205
Conclusions	209
List of Tables	213
List of Figures	215
Bibliography	217
Index	231
About the author	237