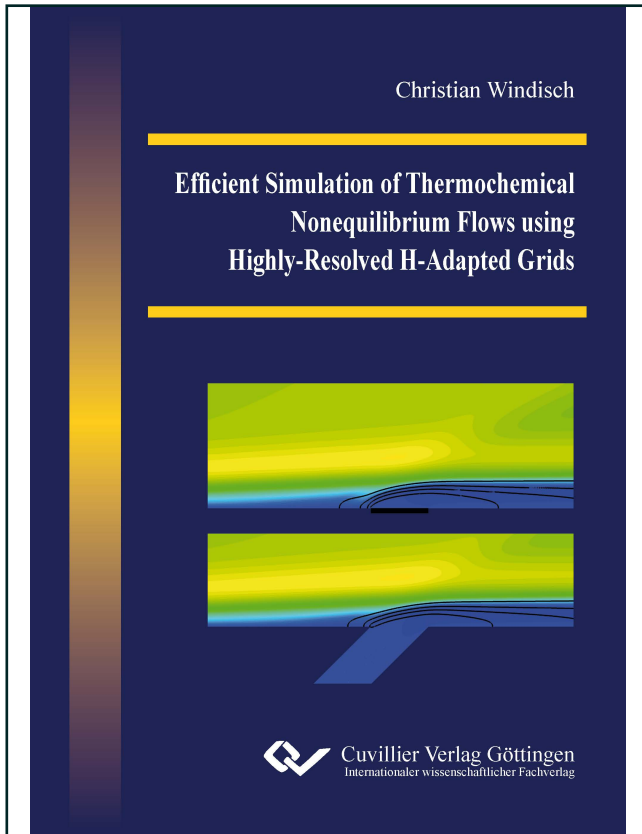




Christian Windisch (Autor)

**Efficient Simulation of Thermochemical
Nonequilibrium Flows using Highly-Resolved H-
Adapted Grids**



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