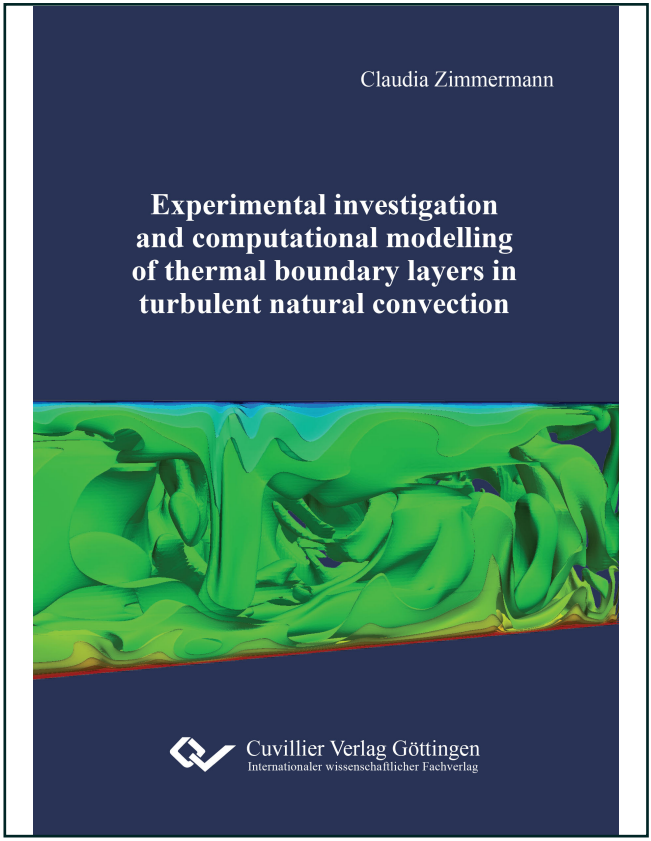
Claudia Zimmermann (Autor)

# Experimental investigation and computational modelling of thermal boundary layers in turbulent natural convection

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